

# NUMERICAL AND EXPERIMENTAL DETERMINATION OF RESIDUAL CONCRETE STRENGTH AFTER ACTION OF FIRE

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## NUMERICAL PROCEDURE FOR RESIDUAL CONCRETE STRENGTH DETERMINATION

### THERMAL ANALYSIS: MODUL "FIRE-T"

Governing differential equation of heat transfer in conduction:

$$\frac{\partial}{\partial x}(\lambda_x \frac{\partial T}{\partial x}) + \frac{\partial}{\partial y}(\lambda_y \frac{\partial T}{\partial y}) + \frac{\partial}{\partial z}(\lambda_z \frac{\partial T}{\partial z}) = \rho c \frac{\partial T}{\partial t}$$

where:

- $\lambda_{x,y,z}$  - is a thermal conductivity (temperature dependent)
- $\rho$  - is a density of the material (temperature dependent)
- $c$  - is a specific heat (temperature dependent)

The heat flow caused by convection:

$$q_c = \alpha_c (T_z - T_f)$$

The heat flow caused by radiation:

$$q_r = V \epsilon \sigma_c (T_{z,a}^4 - T_{f,a}^4) = \alpha_r (T_z - T_f)$$

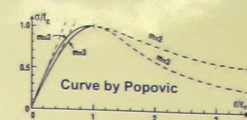
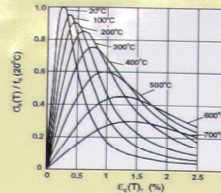
The solution of the differential equation in FEM is:

$$[C] \cdot \dot{\bar{T}} + ([K_1] + [K_2]) \cdot \bar{T} + [R] \cdot \bar{T} = \bar{P}$$

- $[K_1]$  - conductivity matrix (temperature dependent)
- $[K_2]$  - convection matrix
- $[C]$  - capacity matrix (temperature dependent)
- $[R]$  - radiation matrix (temperature dependent)
- $\bar{P}$  - vector of temperature loads (convection and radiation included)
- $\bar{T}$  - vector of unknown nodal temperatures
- $\dot{\bar{T}}$  - vector of temperature derivatives over time

### STRESS-STRAIN LAW FOR CONCRETE AT HIGH TEMPERATURES

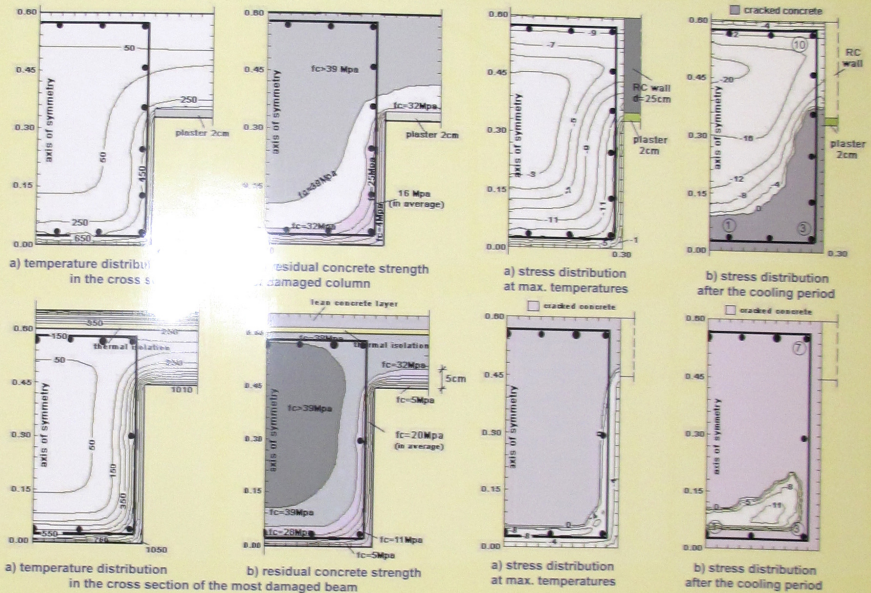
recommended by EC2, Part 1.2



Ascending branch

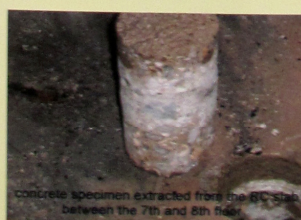
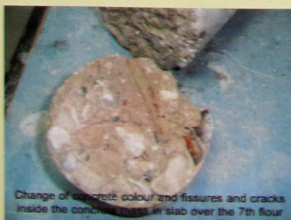
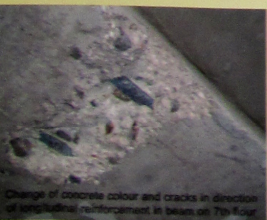
$$\frac{\sigma_c}{f_c} = \frac{\epsilon_c}{\epsilon_{c1}} \cdot \frac{m}{m-1 + (\epsilon_c / \epsilon_{c1})^m}$$

### TEST EXAMPLE FOR NUMERICAL PROCEDURE



## EXPERIMENTAL DETERMINATION OF THE RESIDUAL CONCRETE STRENGTH

Change of concrete colour and deterioration of surface layers of specimens



Concrete strength testing results

Position	Dimensions of specimens (cm)			Concrete compressive strength (MPa)		Concrete strength (MB)
	total H	h (testing)	D	cylinder	reduc.to cube 20/20/20	
RC wall (B8) (after fire expose)	15	9.9	9.9	26.0	26.5	20.0
		3.5		15.8*	16.1	12.0
RC slab (MS) (after fire expose)	18	10.3	9.9	33.8	34.5	26.0
		6.5		12.5*	12.8	9.5
RC slab (SII) (after fire expose)	18	9.6	9.9	38.4	39.1	29.4
		4		13.0*	13.3	10.0
RC wall (V7) (after fire expose)	25	9.9	9.9	35.4	36.1	27.0
		5		14.5*	14.8	11.0
RC wall (G7) (after fire expose)	19.4	10	9.9	25.4	25.9	20.0
		3.5		14.5*	14.5	11.0
RC wall (D7) (after fire expose)	18	10	9.9	30.7	31.3	24.0
		3.5		14.5*	14.8	11.0
RC wall (E7) (after fire expose)	16	10	9.9	31.9	32.6	25.0
		3		14.1	14.4	10.5

\* Values are reduced with coefficients depending on the shape and height (h) of the deteriorated concrete specimens.

Deteriorated concrete specimens, prepared for testing

